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# $(+)_{589}$-Tris-[(-)-trans-1,2-diaminocyclohexane]rhodium(III) Nitrate Trihydrate 

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#### Abstract

Rh}(-\mathrm{chxn})_{3}\right]\left(\mathrm{NO}_{3}\right)_{3} \cdot 3 \mathrm{H}_{2} \mathrm{O}\), hexagonal, $P 6_{3}, \quad a=13.339(2), \quad c=9.848(2) \AA, \quad Z=2, \quad D_{m}=1 \cdot 50$, $D_{x}=1.50 \mathrm{~g} \mathrm{~cm}^{-3}$. The complex ion has a threefold axis of rotation. The rhodium atom is surrounded nearly octahedrally by six nitrogen atoms at an average distance of $2.082(3) \AA$. This is an $o b$ isomer and the central $\mathrm{C}-\mathrm{C}$ bond in the puckered chelate ring is inclined at an angle of $65.9(2)^{\circ}$ to the threefold axis. The absolute configuration can be designated as $\Lambda(\lambda \lambda \lambda)$.


Introduction. The absolute configurations of about 60 complexes had been determined by the end of 1972 and the number is still growing at an increasing rate (Saito, 1974). The X-ray determination of the absolute configuration of transition metal complexes is an elegant means of evaluating many assignments of the chirality of the complex ions on the basis of circular dichroism. About $80 \%$ of the complex ions of which the absolute configurations have been established by means of X-rays are cobalt(III) complexes. The paucity of absolute configurations of complexes of elements other than cobalt is still a distinct handicap. The lel $_{3}$ and $o b_{3}$ isomers of tris-(trans-1,2-diaminocyclohexane)rhodium(III) salts were isolated as chlorides and nitrates and were characterized by their electronic and circular dichroism spectra, optical rotation and thermogravimetry (Galsbøl, Steenbøl \& Sørensen, 1972). The absolute configurations were assigned by correlation of the $\mathrm{lel}_{3}$ isomer with $(-)_{589}-\left[\mathrm{Co}(-\mathrm{chxn})_{3}\right] \mathrm{Cl}_{3} \cdot 5 \mathrm{H}_{2} \mathrm{O}$ using the method of an active racemate, whose absolute configuration was already determined by means of X-rays (Marumo, Utsumi \& Saito, 1970). Crystals of
$(+)_{589}-\left[\mathrm{Rh}(-\mathrm{ch} x n)_{3}\right] \quad\left(\mathrm{NO}_{3}\right)_{3} \cdot 3 \mathrm{H}_{2} \mathrm{O}$ were subjected to X-ray crystal structure analysis in order to verify the absolute configuration and to obtain conformational details.

Crystals of $(+)_{589}-\left[\mathrm{Rh}(-\mathrm{chxn})_{3}\right]\left(\mathrm{NO}_{3}\right)_{3} .3 \mathrm{H}_{2} \mathrm{O}$ (which were kindly supplied by Dr Galsbøl of H. C. Ørsted Institute) are colourless transparent needles. Unit-cell
dimensions were determined from Weissenberg photographs and refined on a diffractometer.

The intensities of reflexions were measured on a Rigaku automated four-circle diffractometer using Mo $K \alpha$ radiation monochromated by a graphite plate. A crystal of dimensions $0.18 \times 0.18 \times 0.19 \mathrm{~mm}$ was used. Of 1750 accessible reflexions below $2 \theta=60^{\circ} 1611$ with $|F| \geq 3 \sigma$ were used for the refinement. The intensity data were corrected for the usual Lorentz and polarization effects. No corrections were made for absorption or extinction.

The structure was solved by routine application of the heavy-atom method and refined by the blockdiagonal least-squares method assuming anisotropic thermal parameters. The $R$ value dropped to 0.038 . At this stage a difference synthesis was calculated and the positions of all the hydrogen atoms except those of the water molecules could be determined. After inclusion of the hydrogen atoms, a final set of leastsquares calculations was carried out assuming isotropic thermal parameters for the hydrogen atoms. The final $R$ value was 0.027 for the 1611 observed reflexions. Unit weight was given to all the reflexions. The scattering factors for all the atoms were those listed in International Tables for X-ray Crystallography (1962). Observed and calculated structure factors are compared in Table 1.* Table 2 lists the final atomic parameters, together with their estimated standard deviations.

Equi-inclination Weissenberg photographs were taken of the zeroth to the third layer lines around the $a$ axis with $\mathrm{Cu} K \alpha$ radiation. Some of the calculated intensities and the observed relations between $h k l$ and its counter-reflexion $h k \bar{l}$ are compared in Table 3. The agreement in the table indicates that the complex ion

* Table 1 has been deposited with the British Library Lending Division as Supplementary Publication No. SUP 30466 ( 9 pp.). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 13 White Friars, Chester CH1 NZ, England.

Table 2. Positional and thermal parameters
(a) Fractional atomic coordinates and thermal parameters for the non-hydrogen atoms ( $\times 10^{4}$ ), with estimated standard deviations. The $\beta_{i j}$ 's are defined by: $\exp \left[-\left(h^{2} \beta_{11}+k^{2} \beta_{22}+l^{2} \beta_{33}+h k \beta_{12}+h l \beta_{13}+k l \beta_{23}\right)\right]$.

|  | $x$ | $y$ | $z$ | $\beta_{11}$ | $\beta_{22}$ | $\beta_{33}$ | $\beta_{12}$ | $\beta_{13}$ | $\beta_{23}$ |
| :--- | :---: | ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Rh | 3333 | 6667 | $0(1)$ | $32(0)$ | $32(0)$ | $38(0)$ | 0 | 0 | 0 |
| $\mathrm{~N}(1)$ | $2179(3)$ | $5213(3)$ | $1122(3)$ | $44(2)$ | $42(2)$ | $56(3)$ | $45(4)$ | $28(5)$ | $3(5)$ |
| $\mathrm{N}(2)$ | $3494(3)$ | $5445(3)$ | $-1135(3)$ | $44(2)$ | $36(2)$ | $56(3)$ | $38(4)$ | $24(5)$ | $-1(4)$ |
| $\mathrm{C}(1)$ | $1886(3)$ | $4165(3)$ | $291(4)$ | $42(2)$ | $35(2)$ | $85(6)$ | $28(4)$ | $34(5)$ | $-3(5)$ |
| $\mathrm{C}(2)$ | $3005(3)$ | $4352(3)$ | $-342(4)$ | $48(3)$ | $34(2)$ | $69(4)$ | $39(4)$ | $32(5)$ | $7(4)$ |
| $\mathrm{C}(3)$ | $2802(4)$ | $3331(4)$ | $-1231(5)$ | $72(4)$ | $41(3)$ | $126(6)$ | $49(6)$ | $66(8)$ | $-19(7)$ |
| $\mathrm{C}(4)$ | $2232(5)$ | $2211(4)$ | $-389(6)$ | $108(5)$ | $41(3)$ | $189(11)$ | $69(6)$ | $109(11)$ | $-2(8)$ |
| $\mathrm{C}(5)$ | $1089(5)$ | $2018(4)$ | $231(11)$ | $91(4)$ | $32(2)$ | $276(16)$ | $14(6)$ | $152(17)$ | $-21(13)$ |
| $\mathrm{C}(6)$ | $1304(4)$ | $3050(4)$ | $1142(5)$ | $78(4)$ | $36(3)$ | $134(6)$ | $35(5)$ | $105(9)$ | $26(7)$ |
| $\mathrm{N}(3)$ | $4822(3)$ | $952(3)$ | $-1054(4)$ | $64(3)$ | $51(3)$ | $86(4)$ | $44(5)$ | $-11(6)$ | $8(6)$ |
| $\mathrm{O}(1)$ | $4737(3)$ | $532(3)$ | $104(6)$ | $99(3)$ | $66(2)$ | $99(4)$ | $58(4)$ | $8(10)$ | $53(9)$ |
| $\mathrm{O}(2)$ | $5080(4)$ | $1979(3)$ | $-1159(3)$ | $198(6)$ | $56(3)$ | $93(4)$ | $106(7)$ | $-27(9)$ | $17(6)$ |
| $\mathrm{O}(3)$ | $4691(4)$ | $370(4)$ | $-2078(4)$ | $142(5)$ | $82(3)$ | $104(4)$ | $124(7)$ | $-39(8)$ | $-45(7)$ |
| $\mathrm{O}(4)$ | $4934(4)$ | $2913(4)$ | $1457(4)$ | $158(5)$ | $98(4)$ | $96(4)$ | $160(8)$ | $-65(8)$ | $-26(7)$ |

Table 2 (cont.)
(b) Positional parameters for the hydrogen atoms with estimated standard deviations ( $\times 10^{3}$ ).
Mean isotropic temperature factor of the hydrogen atoms is $3 \cdot 5(1 \cdot 5) \AA^{2}$.

|  | $x$ | $y$ | $z$ |
| :---: | :---: | :---: | :---: |
| H(1) | 154 (5) | 518 (4) | 146 (6) |
| H(2) | 253 (5) | 511 (5) | 198 (6) |
| H(3) | 417 (4) | 560 (5) | -139 (5) |
| H(4) | 302 (5) | 522 (5) | -202 (6) |
| H(5) | 141 (4) | 410 (4) | -49 (5) |
| H(6) | 355 (4) | 446 (4) | 32 (6) |
| H(7) | 218 (6) | 323 (6) | -227 (7) |
| H(8) | 354 (5) | 350 (5) | -168 (5) |
| H(9) | 206 (6) | 140 (6) | - 126 (7) |
| H(10) | 282 (5) | 219 (6) | 50 (6) |
| H(11) | 42 (6) | 192 (6) | -88 (8) |
| H(12) | 54 (6) | 141 (5) | 1 (12) |
| H(13) | 56 (5) | 275 (5) | 163 (6) |
| H(14) | 191 (5) | 311 (5) | 198 (5) |

shown in Fig. 1 corresponds to $(+)_{589}\left[\mathrm{Rh}(-\mathrm{chxn})_{3}\right]^{3+}$. The absolute configuration can be designated as $\Lambda(\lambda \lambda \lambda)$ according to the IUPAC Information Bulletin (1968), in agreement with the assignment by the method of active racemates (Galsbøl et al., 1973).

Table 3. Determination of the absolute configuration

| $h$ | $k$ | $l$ | $F_{c}^{2}(h k l)$ | Observed <br> relations | $F_{c}^{2}(h k l)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 2 | 1 | 353 | $<$ | 605 |
| 0 | 6 | 4 | 110 | $<$ | 428 |
| 1 | 3 | 2 | 3856 | $<$ | 3069 |
| 1 | 3 | 3 | 467 | $<$ | 824 |
| 2 | 0 | 1 | 353 | $<$ | 707 |
| 2 | 4 | 2 | 2540 | $<$ | 2043 |
| 3 | 1 | 3 | 1303 | $<$ | 1673 |
| 3 | 1 | 1 | 1697 | $>$ | 980 |
| 3 | 2 | 1 | 2314 | $>$ | 1490 |

Discussion. A partial projection of the structure is shown in Fig. 1. The structure consists of the complex cations, nitrate ions and water molecules. The complex
ion has rigorous $C_{3}$ symmetry but has a pseudosymmetry $D_{3}$. The geometry of the complex ion is very similar to that of $(+)_{589}-\left[\mathrm{Co}(-\mathrm{chxn})_{3}\right]^{3+}$ (Kobayashi, Marumo \& Saito, 1972). The bond distances and angles within the complex ion are listed in Table 4. Each ligand molecule is coordinated to the rhodium atom through its nitrogen atoms. The Rh-N distances of $2.089(3)$ and $2.074(3) \AA$ are longer than the $\mathrm{Co}-\mathrm{N}$ distance of $1.984(5) \AA$. The angle $\mathrm{N}-\mathrm{Rh}-\mathrm{N}$ in the chelate ring is reduced to $82 \cdot 7(1)^{\circ}$, being smaller than the corresponding angle of $84 \cdot 3(1)^{\circ}$ in the cobalt analogue. All other bond distances and angles are normal. The cyclohexane ring takes a chair conformation. The $\mathrm{C}-\mathrm{C}$ bonds in the chelate rings are inclined at an angle of $65 \cdot 9(2)^{\circ}$ with respect to the threefold axis. Consequently this is an $o b_{3}$ isomer. The six coordinating nitrogen atoms are slightly distorted from a regular octahedral arrangement. The upper triangle formed by the three nitrogen atoms is rotated counterclockwise by about $5 \cdot 2^{\circ}$ with respect to the lower triangle of the three remaining nitrogen atoms. This is much smaller than the observed angle of $9^{\circ}$ in the cobalt analogue. The $\mathrm{Rh}-\mathrm{N}$ bond is inclined by $58.3(1)^{\circ}$ with respect to the threefold axis of rotation. If the six nitrogen atoms were exactly on the apices of an octahedron this angle would be $54 \cdot 75^{\circ}$. Accordingly


Fig. 1. A partial projection of the structure viewed along the $c$ axis.

Table 4. Interatomic distances and bond angles in the complex ion and the nitrate ion

the $\mathrm{RhN}_{6}$ chromophore is slightly compressed. The corresponding angle in $(+)_{589}-\left[\mathrm{Co}(-\mathrm{chxn})_{3}\right]^{3+}$ is $55 \cdot 2^{\circ}$.

The nitrate ion is almost planar. The average $\mathrm{N}-\mathrm{O}$ distance is $1 \cdot 240(7) \AA$ and the average $\mathrm{O}-\mathrm{N}-\mathrm{O}$ angle is $120 \cdot 0(4)^{\circ}$. The ions are arranged with their planes parallel to, and with $\mathrm{N}-\mathrm{O}(2)$ nearly perpendicular to,

Table 5. Interatomic distances less than $3 \cdot 5 \AA$ outside the complex and the nitrate ions

Key to symmetry operations

| (i) | $x$, | $y$, | $z$ |
| :--- | ---: | ---: | ---: |
| (ii) | $1-y$, | $x-y$, | $z$ |
| (iii) | $1-x+y$, | $1-x$, | $z$ |
| (iv) | $1-x$, | $1-y$, | $-0.5+z$ |
| (v) | $y$, | $1-x+y$, | $0.5+z$ |
| (vi) | $x-y$, | $x$, | $0.5+z$ |
| (vii) | $1-x$, | $-y$, | $-0.5+z$ |
| (viii) | $-y$, | $x-y$, | $z$ |
| (ix) | $x-y$, | $x$, | $-0.5+z$ |


| $\mathrm{N}(1) \cdots \mathrm{O}\left(2^{\text {vi }}\right.$ ) | 2.989 (5) $\AA^{*}$ | $\mathrm{N}(1) \cdots \mathrm{O}\left(1^{\mathrm{viii}}\right)$ | $3 \cdot 321$ (6) A |
| :---: | :---: | :---: | :---: |
| $\mathrm{N}(1) \cdots \mathrm{O}\left(3^{\text {v }}\right.$ ) | $3 \cdot 295$ (7) | $\mathrm{N}(2) \cdots \mathrm{O}\left(4^{\text {lv }}\right.$ ) | $3 \cdot 197$ (5) |
| $\mathrm{N}(2) \cdots \mathrm{O}\left(4^{\text {ix }}\right.$ ) | $2 \cdot 937$ (5)* | $\mathrm{N}(2) \cdots \mathrm{O}\left(1^{\text {iiI }}\right.$ ) | $3 \cdot 422$ (6) |
| $\mathrm{N}(2) \cdots \mathrm{O}\left(3^{\text {iii }}\right)$ | $3 \cdot 149$ (7) | $\mathrm{C}(1) \cdots \mathrm{O}\left(1^{\text {viil }}\right.$ ) | $3 \cdot 258$ (7) |
| $\mathrm{C}(2) \cdots \mathrm{O}\left(1^{\text {III }}\right.$ ) | 3.316 (5) | $\mathrm{O}(1) \cdots \mathrm{O}\left(4^{\text {ii }}\right.$ ) | 3.050 (7) |
| $\mathrm{O}(1) \cdots \mathrm{O}\left(4^{\text {i }}\right.$ ) | 3.333 (7) | $\mathrm{O}(2) \cdots \mathrm{O}\left(4^{\text {i }}\right.$ ) | 2.910 (6)* |
| $\mathrm{O}(2) \cdots \mathrm{O}\left(2^{\text {II }}\right)$ | $3 \cdot 429$ (14) | $\mathrm{O}(3) \cdots \mathrm{O}\left(1^{\text {vii }}\right)$ | $3 \cdot 262$ (7) |
| $\mathrm{O}(4) \cdots \mathrm{O}\left(3^{\text {v1 }}\right)$ | $3 \cdot 211$ (9) |  |  |

* An asterisk indicates hydrogen bonding.
the threefold axis. Pertinent short contacts are listed in Table 5. Hydrogen bonds are formed between amino nitrogen atoms and oxygen atoms of the nitrate ions. They are marked in Table 5 by an asterisk. Although the hydrogen atoms of the water molecule could not be located, the $\mathrm{O}(2) \cdots \mathrm{O}(4)$ distance of $2.910 \AA$ suggests an $\mathrm{O}-\mathrm{H} \cdots \mathrm{O}$ hydrogen bond. Thus the complex cations, water molecules and nitrate ions are linked by a zigzag sequence of hydrogen bonds along the $c$ axis.

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